Non-relativistic effective theory approach to dark matter direct and indirect detection

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Outline

- Introduction
- Effective theory of dark matter-nucleon interactions (Fitzpatrick et. al, 2013)
- Comparison with observations:

Direct Detection:

R. Catena, A. Ibarra, S. Wild, JCAP **1605**, 05, 039 (2016)
R. Catena and P. Gondolo, JCAP **1508**, 08, 022 (2015)
R. Catena, JCAP **1507** 07, 026 (2015)
R. Catena, JCAP **1409**, 09, 049 (2014)
R. Catena and P. Gondolo, JCAP **1409**, 09, 045 (2014)
R. Catena, JCAP **1407**, 07, 055 (2014)

Indirect Detection:

R. Catena, JCAP **1504** 04, 052 (2015)
R. Catena and B. Schwabe JCAP **1504** 04, 042 (2015)

Dark matter direct detection / physical observables

- Rate of dark matter-nucleus scattering events:

$$\frac{\mathrm{d}R}{\mathrm{d}E_R} = \sum_T \xi_T \frac{\rho_\chi}{m_T m_\chi} \int_{v > v_{\min}(q)} f(\mathbf{v} + \mathbf{v}_e(t))\, v\, \frac{\mathrm{d}\sigma_T}{\mathrm{d}E_R}(v^2, q^2)\, d^3v$$

galactic distribution

particle nature

- Modulation amplitude:

$$A(E_-, E_+) = \frac{1}{E_+ - E_-} \frac{1}{2} \left[R(E_-, E_+)\Big|_{\text{June 1st}} - R(E_-, E_+)\Big|_{\text{Dec 1st}} \right]$$

- Standard paradigm: spin-independent and spin-dependent dark matter-nucleon interactions

$$\frac{\mathrm{d}\sigma_T}{\mathrm{d}E_R} = \frac{m_T}{2\pi v^2 [j_\chi][J_T]} \sum_{\mathrm{spins}} \left| \langle F | \sum_{i=1}^{A} e^{-i\mathbf{q}\cdot\mathbf{r}_i} \left(\mathcal{H}_{\mathrm{SI}} + \mathcal{H}_{\mathrm{SD}}\right) | I \rangle \right|^2$$

one-body DM-nucleon interaction

nucleus $\otimes$ DM state

Spin-independent interaction $\mathcal{H}_{\mathrm{SI}}$

- Scalar/Scalar coupling: $\mathcal{L}_{SS} = \frac{1}{\Lambda^3}\sum_q C_q^{SS}\bar{\chi}\chi m_q \bar{q}q$

- **S-matrix element**:

$$\langle f|iS|i\rangle = -i\bar{u}_\chi(p')u_\chi(p)\int d^4x\, e^{i\,qx}\langle N'|\sum_q c_q\bar{q}(x)q(x)|N\rangle$$

$$\simeq -i(2\pi)^4\delta^4(q-k'+k)\,\xi_\chi'^\dagger\xi_\chi\;\xi_N'^\dagger(b_0+b_1\tau_3)\xi_N$$

- Underlying **non-relativistic Hamiltonian**

$$\mathcal{H}_{\mathrm{SI}} = \sum_{\tau=0,1} b_\tau \mathbb{1}_\chi \mathbb{1}_N t^\tau \equiv \sum_{\tau=0,1} c_1^\tau \mathbb{1}_{\chi N}\, t^\tau$$

Spin-dependent interaction $\mathcal{H}_{\mathrm{SD}}$

- Axial-Vector/Axial-Vector: $\mathcal{L}_{AA} = \frac{1}{\Lambda^2} \sum_q C_q^{AA} \bar{\chi}\gamma^\mu\gamma_5\chi\bar{q}\gamma_\mu\gamma_5 q$

- **S-matrix element**:

$$\langle f|iS|i\rangle = -i\bar{u}_\chi(p')\gamma_\mu\gamma_5 u_\chi(p) \int d^4x\, e^{i\,qx} \langle N'| \sum_q c_q \bar{q}(x)\gamma^\mu\gamma_5 q(x)|N\rangle$$
$$\simeq -i(2\pi)^4\delta^4(q-k'+k)\,\xi_\chi'^\dagger \boldsymbol{\sigma}_\chi \xi_\chi \cdot \xi_N'^\dagger(a_0 + a_1\tau_3)\boldsymbol{\sigma}_N \xi_N$$

- Underlying **non-relativistic Hamiltonian**

$$\mathcal{H}_{\mathrm{SD}} = \sum_{\tau=0,1} a_\tau \boldsymbol{\sigma}_\chi \cdot \boldsymbol{\sigma}_N t^\tau \equiv \sum_{\tau=0,1} c_4^\tau \hat{\mathbf{S}}_\chi \cdot \hat{\mathbf{S}}_N t^\tau$$

Effective Theory (ET) of dark matter-nucleon interactions

- It relies on a separation of scales: $|\mathbf{q}|/m_V \ll 1$, where m_V is the mediator mass

- The most general Hamiltonian for χ-N interactions is a power series in $\hat{\mathbf{q}}/m_V$. Each term in the series preserves 3 **fundamental symmetries**, and is a combination of **basic operators**.

- **Fundamental symmetries**: Galilean, rotational and translational invariance

- **Basic operators**:
  - Consider the scattering $\chi(\mathbf{p}) + N(\mathbf{k}) \to \chi(\mathbf{p}') + N(\mathbf{k}')$
  - Momentum conservation $\to \mathcal{M}(\mathbf{p}, \mathbf{k}, \mathbf{q})$
  - Galilean invariance $\to \mathcal{M}(\mathbf{v} = \mathbf{p}/m_\chi - \mathbf{k}/m_N, \mathbf{q})$
  - In general, $\mathcal{M} = \mathcal{M}(\mathbf{v}, \mathbf{q}, \mathbf{S}_\chi, \mathbf{S}_N)$
  - We therefore identify five basic operators

$$\mathbb{1}_{\chi N} \qquad i\hat{\mathbf{q}} \qquad \hat{\mathbf{v}}^\perp = \hat{\mathbf{v}} + \frac{\hat{\mathbf{q}}}{2\mu_N} \qquad \hat{\mathbf{S}}_\chi \qquad \hat{\mathbf{S}}_N$$

- 14 linearly independent operators can be constructed from the basic operators, if we demand that they are at most quadratic in $\hat{\mathbf{q}}$ (and arise from the exchange of a mediator of spin ≤ 1)

- The most general Hamiltonian density is therefore

$$\hat{\mathcal{H}}(\mathbf{r}) = \sum_{\tau=0,1} \sum_{k} c_k^{\tau} \hat{\mathcal{O}}_k(\mathbf{r})\, t^{\tau}$$

- $t^0 = \mathbb{1}$, $t^1 = \tau_3$
- $c_k^p = (c_k^0 + c_k^1)/2$ and $c_k^n = (c_k^0 - c_k^1)/2$

Dark matter-nucleon interaction operators

$\hat{\mathcal{O}}_1 = \mathbb{1}_{\chi N}$	$\hat{\mathcal{O}}_9 = i\hat{\mathbf{S}}_\chi \cdot \left(\hat{\mathbf{S}}_N \times \frac{\hat{\mathbf{q}}}{m_N}\right)$
$\hat{\mathcal{O}}_3 = i\hat{\mathbf{S}}_N \cdot \left(\frac{\hat{\mathbf{q}}}{m_N} \times \hat{\mathbf{v}}^\perp\right)$	$\hat{\mathcal{O}}_{10} = i\hat{\mathbf{S}}_N \cdot \frac{\hat{\mathbf{q}}}{m_N}$
$\hat{\mathcal{O}}_4 = \hat{\mathbf{S}}_\chi \cdot \hat{\mathbf{S}}_N$	$\hat{\mathcal{O}}_{11} = i\hat{\mathbf{S}}_\chi \cdot \frac{\hat{\mathbf{q}}}{m_N}$
$\hat{\mathcal{O}}_5 = i\hat{\mathbf{S}}_\chi \cdot \left(\frac{\hat{\mathbf{q}}}{m_N} \times \hat{\mathbf{v}}^\perp\right)$	$\hat{\mathcal{O}}_{12} = \hat{\mathbf{S}}_\chi \cdot \left(\hat{\mathbf{S}}_N \times \hat{\mathbf{v}}^\perp\right)$
$\hat{\mathcal{O}}_6 = \left(\hat{\mathbf{S}}_\chi \cdot \frac{\hat{\mathbf{q}}}{m_N}\right)\left(\hat{\mathbf{S}}_N \cdot \frac{\hat{\mathbf{q}}}{m_N}\right)$	$\hat{\mathcal{O}}_{13} = i\left(\hat{\mathbf{S}}_\chi \cdot \hat{\mathbf{v}}^\perp\right)\left(\hat{\mathbf{S}}_N \cdot \frac{\hat{\mathbf{q}}}{m_N}\right)$
$\hat{\mathcal{O}}_7 = \hat{\mathbf{S}}_N \cdot \hat{\mathbf{v}}^\perp$	$\hat{\mathcal{O}}_{14} = i\left(\hat{\mathbf{S}}_\chi \cdot \frac{\hat{\mathbf{q}}}{m_N}\right)\left(\hat{\mathbf{S}}_N \cdot \hat{\mathbf{v}}^\perp\right)$
$\hat{\mathcal{O}}_8 = \hat{\mathbf{S}}_\chi \cdot \hat{\mathbf{v}}^\perp$	$\hat{\mathcal{O}}_{15} = -\left(\hat{\mathbf{S}}_\chi \cdot \frac{\hat{\mathbf{q}}}{m_N}\right)\left[\left(\hat{\mathbf{S}}_N \times \hat{\mathbf{v}}^\perp\right) \cdot \frac{\hat{\mathbf{q}}}{m_N}\right]$

Dark matter-nucleus scattering cross-section

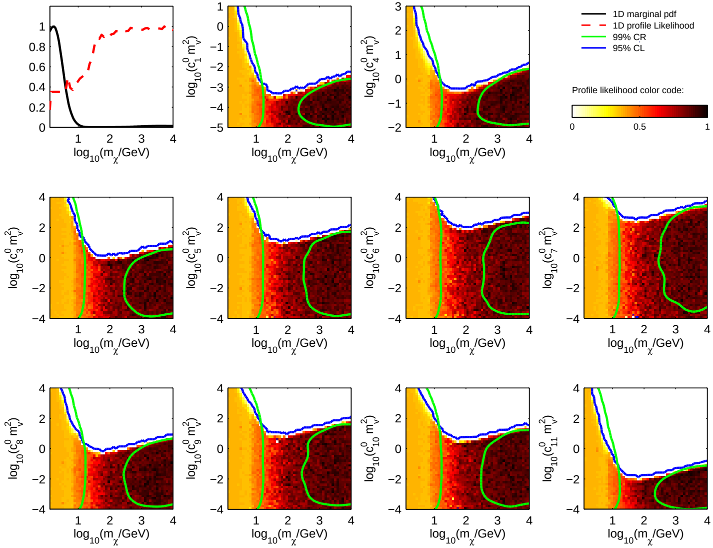
- In the ET framework, the dark matter-nucleus scattering cross-section is

$$\frac{\mathrm{d}\sigma_T}{\mathrm{d}E_R} = \frac{m_T}{2\pi v^2[j_\chi][J_T]} \sum_{\text{spins}} \left| \langle F | \sum_{i=1}^{A} \int \mathrm{d}\mathbf{r}\, e^{-i\mathbf{q}\cdot\mathbf{r}} \hat{\mathcal{H}}_i(\mathbf{r}) | I \rangle \right|^2$$

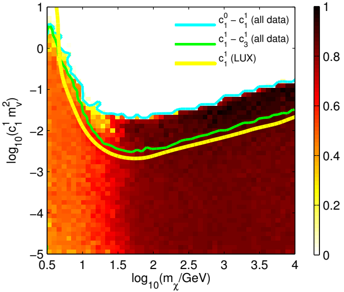
- This expression depends on:
  - 28 coupling constants
  - 8 nuclear response functions
- Available nuclear response functions, e.g.:
  - For Xe, Ge, I, Na, F: Anand et al. 2013
  - For 16 elements in the Sun: R. Catena & B. Schwabe 2015

Global limits: mass vs coupling constants

R. Catena and P. Gondolo, JCAP **1409** (2014) 045



R. Catena and P. Gondolo, JCAP **1508**, 08, 022 (2015)

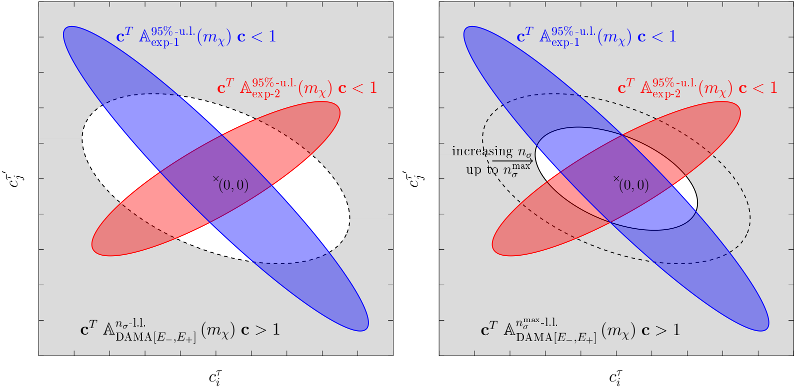


- Pairs of operators, or isoscalar and isovector components of the same operator can interfere
- For instance, the operators $\hat{\mathcal{O}}_1$ and $\hat{\mathcal{O}}_3$ generate a transition probability proportional to

$$\mathcal{P}^{c_1 c_3} \propto \sum_{\tau\tau'} \Big[c_1^\tau c_1^{\tau'} W_M^{\tau\tau'}(q) + \frac{1}{8}\frac{q^2}{m_N^2} v_T^{\perp 2} c_3^\tau c_3^{\tau'} W_{\Sigma'}^{\tau\tau'}(q) + \frac{q^2}{m_N^2}\left(\frac{q^2}{4m_N^2} c_3^\tau c_3^{\tau'} W_{\Phi''}^{\tau\tau'}(q) + c_1^\tau c_3^{\tau'} W_{\Phi'' M}^{\tau\tau'}(q) \right) \Big]$$

DAMA confronts null searches I

Is there a linear combination of $\hat{\mathcal{O}}_k$ such that DAMA can be reconciled with null searches?



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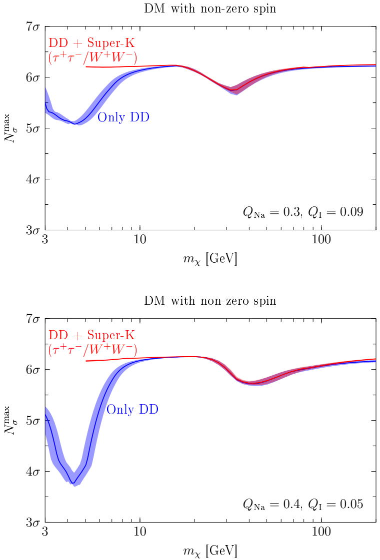
DAMA confronts null searches II



Neutrino telescopes: highlights

R. Catena, JCAP **1504** 04, 052 (2015)

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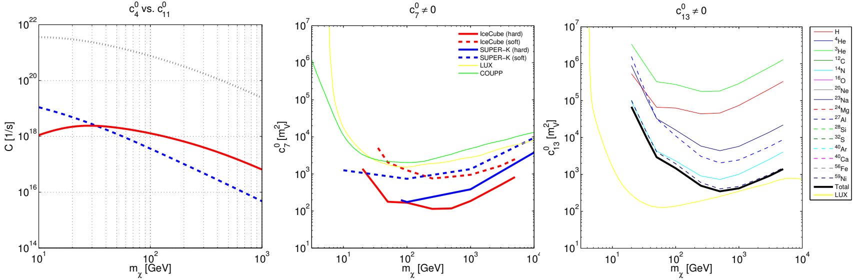

- $\hat{\mathcal{O}}_4 = \hat{\mathbf{S}}_\chi \cdot \hat{\mathbf{S}}_N$, $\hat{\mathcal{O}}_{11} = i\hat{\mathbf{S}}_\chi \cdot \hat{\mathbf{q}}/m_N$
- $\hat{\mathcal{O}}_7 = \hat{\mathbf{S}}_N \cdot \hat{\mathbf{v}}^\perp$
- $\hat{\mathcal{O}}_{13} = i\left(\hat{\mathbf{S}}_\chi \cdot \hat{\mathbf{v}}^\perp\right)\left(\hat{\mathbf{S}}_N \cdot \frac{\hat{\mathbf{q}}}{m_N}\right)$

Conclusions

- A complete classification of all one-body dark matter-nucleon interaction operators has recently been performed
- Current direct detection data place interesting constraints on dark matter-nucleon interaction operators commonly neglected
- Destructive interference effects can weaken standard direct detection exclusion limits by up to 1 order of magnitude in the coupling constants
- Even within this general theoretical framework, it seems to be difficult to reconcile DAMA with null searches